

STUDENT ID NO										

MULTIMEDIA UNIVERSITY

FINAL EXAMINATION

TRIMESTER 2, 2018/2019

DEM5028 - ENGINEERING MATHEMATICS 2

(Diploma in Electronic Engineering)

4 MARCH 2019 2.30 PM – 4.30 PM (2 Hours)

INSTRUCTIONS TO STUDENT

- 1. This question paper consists of 3 pages (excluding the cover page and appendices).
- 2. Attempt ALL FOUR questions.
- 3. Write your answers in the answer booklet provided.
- 4. Formulae are provided in the appendix section.

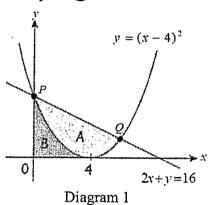
QUESTION 1

a. Evaluate the following integrals.

i.
$$\int \frac{5x^2 + 20x + 6}{x^3 + 2x^2 + x} dx$$
 (8 marks)

ii.
$$\int_0^{\frac{\pi}{4}} x \sec^2 x \, dx \tag{5 marks}$$

b. The Diagram 1 below shows a straight line 2x + y = 16 intersecting a curve $y = (x - 4)^2$ at point P and point Q. Find



i. the area of the region A.

(8 marks)

ii. the volume generated when the shaded region B is revolved through 360° about the x-axis. (4 marks)

[TOTAL 25 MARKS]

QUESTION 2

- a. Find the general solution of the differential equation $2 + \frac{dy}{dx} = \frac{3x}{y-2} + 2$. (5 marks)
- b. Find the solution of the differential equation $y^2 \frac{dy}{dx} = -3y\sqrt{x}$, given that y = 1 when x = 1. (9 marks)
- c. Find the solution of differential equation $x \frac{dy}{dx} x^4 = -y$, subject to y(1) = 1. (11 marks)

[TOTAL 25 MARKS]

QUESTION 3

- a. Find the sum to infinity for the series 18-6+2-... (4 marks)
- b. Expand $(9+x)^{\frac{1}{2}}$ in ascending powers of x up to the term in x^2 . (7 marks)
- c. Given that A(3,-1,1), B(-1,2,-2) and C(3,2,-2) are three vertices of a triangle
 - i. Find $\overrightarrow{AB} \times \overrightarrow{BC}$. (7 marks)
 - ii. Calculate the area of triangle ABC. (7 marks)

[TOTAL 25 MARKS]

QUESTION 4

- a. If $f(x, y) = e^{2x} \sin(3x + 2y)$.
 - i. Compute $\frac{\partial f}{\partial x}\Big|_{\left(0,\frac{1}{8}\pi\right)}$ and $\frac{\partial f}{\partial y}\Big|_{\left(0,\frac{1}{8}\pi\right)}$. (9 marks)
 - ii. Evaluate f_{xx} and f_{yy} . (8 marks)
 - b. Find the volume of the solid bounded above by the plane z=4-x-y and below by the rectangle $R=\{(x,y):0\leq x\leq 1\,,\,0\leq y\leq 2\}$. (8 marks)

[TOTAL 25 MARKS]

APPENDICES: Formulae

Integration of common functions

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C \qquad \int \frac{1}{x} dx = \ln|x| + C \qquad \int e^x dx = e^x + C \qquad \int a^x dx = \frac{a^x}{\ln a} + C$$

$$\int \sin x dx = -\cos x + C \qquad \int \cos x dx = \sin x + C \qquad \int \sec^2 x dx = \tan x + C \qquad \int \sec x \tan x dx = \sec x + C$$

$$\int \csc^2 x dx = -\cot x + C \qquad \int \csc x \cot x dx = -\csc x + C$$

Inverse Trigonometry

Pythagorean Identities

Integration by parts

$$\int \frac{1}{\sqrt{1-x^2}} dx = \sin^{-1} x + C$$
$$\int \frac{1}{x^2 + 1} dx = \tan^{-1} x + C$$

$$\sin^2 x + \cos^2 x = 1$$
$$1 + \cot^2 x = \csc^2 x$$
$$1 + \tan^2 x = \sec^2 x$$

$$\int u dv = uv - \int v du$$

Areas Between Curves

Volume by Cylindrical Shells

$$A = \int_{a} [f(x) - g(x)] dx$$

$$A = \int_{a}^{b} [f(x) - g(x)] dx \qquad V = \int_{a}^{b} \pi ([f(x)]^{2} - [g(x)]^{2}) dx \qquad V = \int_{a}^{b} 2\pi x (f(x) - g(x)) dx$$

$$V = \int_a^b 2\pi x (f(x) - g(x)) dx$$

$$A = \int_{c}^{d} [w(y) - v(y)] dy$$

$$A = \int_{c}^{d} [w(y) - v(y)] dy \qquad V = \int_{c}^{d} \pi ([w(y)]^{2} - [v(y)]^{2}) dy \qquad V = \int_{c}^{d} 2\pi y (w(y) - v(y)) dy$$

$$V = \int_{c}^{d} 2\pi y (w(y) - v(y)) dy$$

Linear Differential Equations:

$$\frac{dy}{dx} + p(x)y = q(x); \ \mu y = \int \mu q(x) dx \Rightarrow y = \frac{1}{\mu} \int \mu q(x) dx, \quad \text{where } \mu = e^{\int p(x) dx}$$

where
$$\mu = e^{\int p(x)dx}$$

Divergence Test	If $\lim_{n\to\infty} a_n \neq 0$, then $\sum a_n$ diverges.					
p-series	The p-series $\sum_{n=1}^{\infty} \frac{1}{n^p}$ is convergent if $p > 1$ and divergent if $p \le 1$.					
Limit Comparison Test	Let $\sum a_n$ and $\sum b_n$ be series with positive terms such that $\lim_{n\to\infty} \frac{a_n}{b_n} = c$					
	If $0 < c < \infty$, then both series converge or both diverge.					
Alternating Series Test	If the alternating series $\sum_{n=1}^{\infty} (-1)^{n-1} b_n = b_1 - b_2 + b_3 - b_4 + \dots \qquad b_n > 0$ Satisfies: i. $b_{n+1} \le b_n$ for all n					
	satisfies. I. $b_{n+1} \le b_n$ for all n ii. $\lim_{n \to \infty} b_n = 0$ then the series is convergent					
Ratio Test	Let $\sum a_n$ be a series with nonzero terms such that $L = \lim_{n \to \infty} \frac{ a_{n+1} }{ a_n }$					
	 a. Series converges absolutely if L < 1 b. Series diverges if L > 1 or L = ∞ c. No conclusion if L = 1 					

TCF

Binomial expansion

$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^{n-k} b^k$$

Vector

The length of the vector $\mathbf{a} = \langle a_1, a_2, a_3 \rangle$ is $|a| = \sqrt{{a_1}^2 + {a_2}^2 + {a_3}^2}$.

If θ is the angle between the vector \mathbf{a} and \mathbf{b} , then $\mathbf{a.b} = |\mathbf{a}||\mathbf{b}|\cos\theta \& |\mathbf{a} \times \mathbf{b}| = |\mathbf{a}||\mathbf{b}|\sin\theta$

Cross Product

$$\mathbf{a} \times \mathbf{b} = \begin{vmatrix} i & j & k \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix} = \begin{vmatrix} a_2 & a_3 \\ b_2 & b_3 \end{vmatrix} i - \begin{vmatrix} a_1 & a_3 \\ b_1 & b_3 \end{vmatrix} j + \begin{vmatrix} a_1 & a_2 \\ b_1 & b_2 \end{vmatrix} k$$

Equation of Line

Vector equation: $r = r_0 + tv$

Parametric equation: $x = x_0 + at$, $y = y_0 + bt$, $z = z_0 + ct$

Equation of Plane $\langle a,b,c \rangle \langle x-x_0,y-y_0,z-z_0 \rangle = 0$

The Chain Rule

Suppose that
$$z = f(x, y)$$
, where $x = g(t)$ and $y = h(t)$ \Rightarrow $\frac{dz}{dt} = \frac{\partial f}{\partial x} \frac{dx}{dt} + \frac{\partial f}{\partial y} \frac{dy}{dt}$

Second Derivatives Test

Suppose that $f_x(a,b) = 0$ and $f_y(a,b) = 0$ [that is, (a,b) is a critical point of f]. Let $D = D(a,b) = f_{xx}(a,b)f_{yy}(a,b) - [f_{xy}(a,b)]^2$

- a. If D > 0 and $f_{xx}(a,b) > 0$, then f(a,b) is a local minimum.
- b. If D > 0 and $f_{xx}(a,b) < 0$, then f(a,b) is a local maximum
- c. If D < 0, then f(a, b) is a saddle point.

Moments and Centers of Mass

The moment about the x-axis:

$$M_x = \iint_D y \rho(x, y) dA$$

The moment about the y-axis:

$$M_{y} = \iint_{D} x \rho(x, y) dA$$

The coordinates (x, y) of the center of mass:

$$\overline{x} = \frac{M_y}{m} = \frac{1}{m} \iint_D x \rho(x, y) dA \qquad \overline{y} = \frac{M_x}{m} = \frac{1}{m} \iint_D y \rho(x, y) dA \qquad \text{Where the mass:}$$

$$m = \iint_D \rho(x, y) dA$$

Triple Integrals:
$$\iiint_B f(x, y, z) dV = \int_r^s \int_c^d \int_a^b f(x, y, z) dx dy dz$$